

Model Equations

The general form of the time rate of change equations are:

$$\frac{D(NO_3)}{Dt} = \eta NH_4 - \frac{V_{sp}^{NO_3}}{V_{sp}^{N_{tot}}} PC_{sp}^{photo} SP_C Q - \frac{V_{diat}^{NO_3}}{V_{diat}^{N_{tot}}} PC_{diat}^{photo} Diat_C Q - (r DOC + POC^{remin}) R_{denitrif}^{C:N} \quad (1)$$

$$\begin{aligned} \frac{D(NH_4)}{Dt} = & -\eta NH_4 - \frac{V_{sp}^{NH_4}}{V_{sp}^{N_{tot}}} PC_{sp}^{photo} SP_C Q - \frac{V_{diat}^{NH_4}}{V_{diat}^{N_{tot}}} PC_{diat}^{photo} Diat_C Q + r DON \\ & + (Z_{loss}^{DIC} + SP_{loss}^{DIC} + G_{sp}^{DIC} + Diat_{loss}^{DIC} + G_{diat}^{DIC} + POC^{remin} + Diaz_{loss}^{DIC} + G_{diaz}^{DIC}) Q \end{aligned} \quad (2)$$

$$\begin{aligned} \frac{D(Fe)}{Dt} = & PFe^{remin} + Z_{loss}^{DIC} Q_Z^{Fe} + r DOFe + (SP_{loss}^{DIC} + G_{sp}^{DIC}) Q_{sp}^{Fe} + (Diat_{loss}^{DIC} + G_{diat}^{DIC}) Q_{diat}^{Fe} \\ & + (Diaz_{loss}^{DIC} + G_{diaz}^{DIC}) Q_{diaz}^{Fe} + G_{diaz}^Z (Q_{diaz}^{Fe} - Q_Z^{Fe}) + G_{diat}^Z (Q_{diat}^{Fe} - Q_Z^{Fe}) + G_{sp}^Z (Q_{sp}^{Fe} - Q_Z^{Fe}) \\ & - PC_{sp}^{photo} SP_C Q_{sp}^{Fe} - PC_{diat}^{photo} Diat_C Q_{diat}^{Fe} - PC_{diaz}^{photo} Diaz_C Q_{diaz}^{Fe} - s^{Fe} Fe \end{aligned} \quad (3)$$

$$\frac{D(SiO_3)}{Dt} = PSiO_3^{remin} + (f_{graz}^{Si,rem} G_{diat} + f_{diat}^{DOC} Diat_{loss}) Q_{diat}^{Si} - PC_{diat}^{photo} Diat_C Q_{diat}^{Si} \quad (4)$$

$$\begin{aligned} \frac{D(PO_4)}{Dt} = & (POC^{remin} + Z_{loss}^{DIC} + SP_{loss}^{DIC} + G_{sp}^{DIC} + Diat_{loss}^{DIC} + G_{diat}^{DIC} - PC_{sp}^{photo} SP_C - PC_{diat}^{photo} Diat_C) Q^P \\ & + r DOP + Diaz_{loss}^{DIP} - PC_{diaz}^{photo} Diaz_C Q_{diaz}^P \end{aligned} \quad (5)$$

$$\frac{D(SP_C)}{Dt} = PC_{sp}^{photo} SP_C - G_{sp} - SP_{loss} - SP_{agg} \quad (6)$$

$$\frac{D(SP_{Chl})}{Dt} = \frac{\rho_{sp}^{Chl} PC_{sp}^{photo} Q}{\theta_{sp}^C} SP_{Chl} - (G_{sp} + SP_{loss} + SP_{agg}) \theta_{sp}^C \quad (7)$$

$$\frac{D(SP_{CaCO_3})}{Dt} = f_{prod}^{sp,CaCO_3} PC_{sp}^{photo} SP_C - (G_{sp} + SP_{loss} + SP_{agg}) Q_{sp}^{CaCO_3} \quad (8)$$

$$\frac{D(Diat_C)}{Dt} = PC_{diat}^{photo} Diat_C - G_{diat} - Diat_{loss} - Diat_{agg} \quad (9)$$

$$\frac{D(Diat_{Chl})}{Dt} = \frac{\rho_{diat}^{Chl} PC_{diat}^{photo} Q}{\theta_{diat}^C} Diat_{Chl} - (G_{diat} + Diat_{loss} + Diat_{agg}) \theta_{diat}^C \quad (10)$$

$$\frac{D(Z_C)}{Dt} = G_{sp}^Z + G_{diat}^Z + G_{diaz}^Z - Z_{loss} \quad (11)$$

$$\frac{D(DOC)}{Dt} = SP_{loss}^{DOC} + G_{sp}^{DOC} + Z_{loss}^{DOC} + Diat_{loss}^{DOC} + G_{diat}^{DOC} + Diaz_{loss}^{DOC} + G_{diaz}^{DOC} - r DOC \quad (12)$$

$$\begin{aligned} \frac{D(DON)}{Dt} = & (SP_{loss}^{DOC} + G_{sp}^{DOC} + Z_{loss}^{DOC} + Diat_{loss}^{DOC} + G_{diat}^{DOC} + Diaz_{loss}^{DOC} + G_{diaz}^{DOC}) Q - r DON \\ & + (\zeta_C^N - 1) PC_{diaz}^{photo} Diaz_C Q \end{aligned} \quad (13)$$

$$\frac{D(DOP)}{Dt} = (SP_{loss}^{DOC} + G_{sp}^{DOC} + Z_{loss}^{DOC} + Diat_{loss}^{DOC} + G_{diat}^{DOC}) Q^P + Diaz_{loss}^{DOP} - r DOP \quad (14)$$

$$\begin{aligned} \frac{D(DOFe)}{Dt} = & Z_{loss}^{DOC} Q_Z^{Fe} + (G_{sp}^{DOC} + SP_{loss}^{DOC}) Q_{sp}^{Fe} + (G_{diat}^{DOC} + Diat_{loss}^{DOC}) Q_{diat}^{Fe} + (G_{diaz}^{DOC} + Diaz_{loss}^{DOC}) Q_{diaz}^{Fe} \\ & - r DOFe \end{aligned} \quad (15)$$

$$\frac{D(SP_{Fe})}{Dt} = PC_{sp}^{photo} SP_C Q_{sp}^{Fe} - (G_{sp} + SP_{loss} + SP_{agg}) Q_{sp}^{Fe} \quad (16)$$

$$\frac{D(\text{Diat}_{Fe})}{Dt} = PC_{diat}^{photo} \text{Diat}_C \theta_{diat}^{Fe} Q_{diat}^{Fe} - (G_{diat} + \text{Diat}_{loss} + \text{Diat}_{agg}) Q_{Diat}^{Fe} \quad (17)$$

$$\frac{D(\text{Diat}_{Si})}{Dt} = PC_{diat}^{photo} \text{Diat}_C \theta_{diat}^{Si} Q_{diat}^{Si} - (G_{diat} + \text{Diat}_{loss} + \text{Diat}_{agg}) Q_{Diat}^{Si} \quad (18)$$

$$\frac{D(\text{Diaz}_C)}{Dt} = PC_{diat}^{photo} \text{Diaz}_C - G_{diat} - \text{Diaz}_{loss} \quad (19)$$

$$\frac{D(\text{Diaz}_{Chl})}{Dt} = \frac{\rho_{diat}^{Chl} PC_{diat}^{photo} Q}{\theta_{diat}^C} \text{Diaz}_{Chl} - \theta_{diat}^C (G_{diat} + \text{Diaz}_{loss}) \quad (20)$$

$$\frac{D(\text{Diaz}_{Fe})}{Dt} = PC_{diat}^{photo} \text{Diaz}_C \theta_{diat}^{Fe} Q_{diat}^{Fe} - (G_{diat} + \text{Diaz}_{loss}) Q_{Diat}^{Fe} \quad (21)$$

$$\begin{aligned} \frac{D(\text{DIC})}{Dt} = & r \text{DOC} + \text{POC}^{remin} + \text{PCaCO}_3^{remin} + f_{graz}^{\text{CaCO}_3, remin} G_{sp} Q_{sp}^{\text{CaCO}_3} + Z_{loss}^{DIC} + \text{SP}_{loss}^{DIC} + G_{sp}^{DIC} \\ & + \text{Diat}_{loss}^{DIC} + G_{diat}^{DIC} + \text{Diaz}_{loss}^{DIC} + G_{diat}^{DIC} - PC_{sp}^{photo} \text{SP}_C - PC_{diat}^{photo} \text{Diat}_C - PC_{diat}^{photo} \text{Diaz}_C \\ & - f_{prod}^{\text{sp, CaCO}_3} PC_{sp}^{photo} \text{SP}_C F_{nut} \end{aligned} \quad (22)$$

$$\begin{aligned} \frac{D(\text{ALK})}{Dt} = & 2 \left(\text{PCaCO}_3^{remin} + f_{graz}^{\text{CaCO}_3, remin} G_{sp} Q_{sp}^{\text{CaCO}_3} - f_{prod}^{\text{sp, CaCO}_3} PC_{sp}^{photo} \text{SP}_C F_{nut} \right) - \frac{D(\text{NO}_3)}{Dt} \\ & + \frac{D(\text{NH}_4)}{Dt} \end{aligned} \quad (23)$$

$$\begin{aligned} \frac{D(\text{O}_2)}{Dt} = & \frac{PC_{sp}^{photo} \text{SP}_C + PC_{diat}^{photo} \text{Diat}_C}{R_D^{C:O_2}} + \frac{PC_{diat}^{photo} \text{Diaz}_C}{diat R_D^{C:O_2}} \\ & - \left(\frac{\text{POC}^{remin} + r \text{DOC} + Z_{loss}^{DIC} + \text{SP}_{loss}^{DIC} + \text{Diat}_{loss}^{DIC} + \text{Diaz}_{loss}^{DIC} + G_{sp}^{DIC} + G_{diat}^{DIC} + G_{diat}^{DIC}}{R_P^{C:O_2}} \right) \end{aligned} \quad (24)$$

Where:

$$V_{sp}^{NO_3} = \frac{\frac{NO_3}{K_{sp}^{NO_3}}}{\left(1 + \frac{NO_3}{K_{sp}^{NO_3}} + \frac{NH_4}{K_{sp}^{NH_4}}\right)}; \quad V_{sp}^{NH_4} = \frac{\frac{NH_4}{K_{sp}^{NH_4}}}{\left(1 + \frac{NO_3}{K_{sp}^{NO_3}} + \frac{NH_4}{K_{sp}^{NH_4}}\right)}; \quad V_{sp}^{N_{tot}} = V_{sp}^{NO_3} + V_{sp}^{NH_4}$$

$$V_{diat}^{NO_3} = \frac{\frac{NO_3}{K_{diat}^{NO_3}}}{\left(1 + \frac{NO_3}{K_{diat}^{NO_3}} + \frac{NH_4}{K_{diat}^{NH_4}}\right)}; \quad V_{diat}^{NH_4} = \frac{\frac{NH_4}{K_{diat}^{NH_4}}}{\left(1 + \frac{NO_3}{K_{diat}^{NO_3}} + \frac{NH_4}{K_{diat}^{NH_4}}\right)}; \quad V_{diat}^{N_{tot}} = V_{diat}^{NO_3} + V_{diat}^{NH_4}$$

$$V_{sp}^{Fe} = \frac{Fe}{Fe + K_{sp}^{Fe}}; \quad V_{sp}^{PO_4} = \frac{PO_4}{PO_4 + K_{sp}^{PO_4}}$$

$$V_{diat}^{Fe} = \frac{Fe}{Fe + K_{diat}^{Fe}}; \quad V_{diat}^{PO_4} = \frac{PO_4}{PO_4 + K_{diat}^{PO_4}}; \quad V_{diat}^{SiO_3} = \frac{SiO_3}{SiO_3 + K_{diat}^{SiO_3}}$$

$$V_{diat}^{Fe} = \frac{Fe}{Fe + K_{diat}^{Fe}}; \quad V_{diat}^{PO_4} = \frac{PO_4}{PO_4 + K_{diat}^{PO_4}}$$

$$PC_{sp}^{photo} = PC_{sp}^{max} \left(1 - e^{-\frac{\alpha \theta_{sp}^C I_{PAR}}{PC_{sp}^{max}}}\right); \quad PC_{diat}^{photo} = PC_{diat}^{max} \left(1 - e^{-\frac{\alpha \theta_{diat}^C I_{PAR}}{PC_{diat}^{max}}}\right); \quad PC_{diat}^{photo} = PC_{diat}^{max} \left(1 - e^{-\frac{\alpha_{diat} \theta_{diat}^C I_{PAR}}{PC_{diat}^{max}}}\right);$$

$$PC_{sp}^{max} = PC_{sp}^{ref} F_{sp}^{nut} T_f; \quad PC_{diat}^{max} = PC_{diat}^{ref} F_{diat}^{nut} T_f; \quad PC_{diat}^{max} = PC_{diat}^{ref} F_{diat}^{nut} T_f;$$

$$F_{sp}^{nut} = \text{MIN}(V_{sp}^{N_{tot}}, V_{sp}^{Fe}, V_{sp}^{PO_4}); \quad F_{diat}^{nut} = \text{MIN}(V_{diat}^{N_{tot}}, V_{diat}^{Fe}, V_{diat}^{PO_4}, V_{diat}^{SiO_3}); \quad F_{diat}^{nut} = \text{MIN}(V_{diat}^{Fe}, V_{diat}^{PO_4})$$

$$T_f = q_{10}^{\frac{(T+T_{K0}) - (T_{ref}+T_{K0})}{10}}$$

$$I_{PAR} = I_0 \phi e^{-(\kappa_w + \kappa_{chl} (SP_{Chl} + Diat_{Chl} + Diaz_{Chl})) z}$$

$$Z_{loss}^{DOC} = (1 - f_{DOC}^{lab}) (1 - F_Z^{POC}) Z_{loss}; \quad Z_{loss}^{DIC} = f_{DOC}^{lab} (1 - F_Z^{POC}) Z_{loss}$$

$$Z_{loss} = T_f (m_z Z_C + p_z Z_C^2)$$

$$F_Z^{POC} = \frac{f_{z_{loss}}^{sp,POC} G_{sp} + f_{z_{loss}}^{diat,POC} G_{diat} + f_{z_{loss}}^{diaz,POC} G_{diaz}}{G_{sp} + G_{diat} + G_{diaz}}$$

$$G_{sp} = u_{max}^{sp} T_f \left(\frac{SP_C^2}{SP_C^2 + g^2} \right) Z_C; \quad G_{diat} = u_{max}^{diat} T_f \left(\frac{Diat_C^2}{Diat_C^2 + g^2 f_z^{diat}} \right) Z_C; \quad G_{diaz} = u_{max}^{diaz} T_f \left(\frac{Diaz_C^2}{Diaz_C^2 + g^2} \right) Z_C$$

$$SP_{loss} = m_{sp} SP_C; \quad Diat_{loss} = m_{diat} Diat_C; \quad Diaz_{loss} = m_{diaz} Diaz_C$$

$$SP_{loss}^{POC} = Q_{sp}^{CaCO_3} SP_{loss}; \quad SP_{loss}^{DOC} = (1 - f_{DOC}^{lab}) (SP_{loss} - SP_{loss}^{POC}); \quad SP_{loss}^{DIC} = f_{DOC}^{lab} (SP_{loss} - SP_{loss}^{POC})$$

$$Diat_{loss}^{POC} = f_{diat_{loss}}^{POC} Diat_{loss}; \quad Diat_{loss}^{DOC} = (1 - f_{DOC}^{lab}) f_{diat_{loss}}^{DOC} Diat_{loss}; \quad Diat_{loss}^{DIC} = f_{DOC}^{lab} f_{diat_{loss}}^{DOC} Diat_{loss}$$

$$Diaz_{loss}^{DOC} = (1 - f_{DOC}^{lab}) Diaz_{loss}; \quad Diaz_{loss}^{DIC} = f_{DOC}^{lab} Diaz_{loss}$$

$$Diaz_{loss}^{DOP} = (1 - f_{DOC}^{lab}) Diaz_P^{remain}; \quad Diaz_{loss}^{DIP} = f_{DOC}^{lab} Diaz_P^{remain}$$

$$Diaz_P^{remain} = (G_{diaz} + Diaz_{loss}) Q_{diaz}^P - (G_{diaz}^{POC} + G_{diaz}^Z) Q^P$$

$$SP_{agg} = MIN(a_{sp}^{max} SP_C, p_{sp} SP_C^2); \quad Diat_{agg} = MIN(a_{diat}^{max} Diat_C, p_{diat} Diat_C^2)$$

$$G_{sp}^Z = i_z G_{sp}; \quad G_{sp}^{POC} = G_{sp} \times MAX(f_{graz}^{CaCO_3,POC} Q_{sp}^{CaCO_3}, MIN(e_{sp}^{POC} SP_C, f_{graz}^{sp,POC})); \quad G_{diat}^Z = i_z G_{diat}; \quad G_{diat}^{POC} = f_{graz}^{diat,POC} G_{diat}; \quad G_{diaz}^Z = f_{graz}^{diaz,Z} G_{diaz}; \quad G_{diaz}^{POC} = f_{graz}^{diaz,POC} G_{diaz};$$

$$G_{sp}^{DOC} = f_{graz}^{sp,DOC} G_{sp} - G_{sp}^{POC}; \quad G_{diat}^{DOC} = f_{graz}^{diat,DOC} G_{diat}; \quad G_{diaz}^{DOC} = f_{graz}^{diaz,DOC} G_{diaz};$$

$$G_{sp}^{DIC} = f_{graz}^{sp,DIC} G_{sp}; \quad G_{diat}^{DIC} = f_{graz}^{diat,DIC} G_{diat}; \quad G_{diaz}^{DIC} = f_{graz}^{diaz,DIC} G_{diaz};$$

$$\theta_{sp}^C = \frac{SP_{Chl}}{SP_C}; \quad \theta_{diat}^C = \frac{Diat_{Chl}}{Diat_C}; \quad \theta_{diaz}^C = \frac{Diaz_{Chl}}{Diaz_C}$$

$$Q_{sp}^{Fe} = \frac{SP_{Fe}}{SP_C}; \quad Q_{sp}^{CaCO_3} = \frac{SP_{CaCO_3}}{SP_C}; \quad Q_{diaz}^{Fe} = \frac{Diaz_{Fe}}{Diaz_C}$$

$$Q_{diat}^{Fe} = \frac{Diat_{Fe}}{Diat_C}; \quad Q_{diat}^{Si} = \frac{Diat_{Si}}{Diat_C};$$

$$\rho_{sp}^{Chl} = \max \theta_{sp}^N \frac{PC_{sp}^{photo}}{\alpha \theta_{sp}^C I_{PAR}}; \quad \rho_{diat}^{Chl} = \max \theta_{diat}^N \frac{PC_{diat}^{photo}}{\alpha \theta_{diat}^C I_{PAR}}; \quad \rho_{diaz}^{Chl} = \max \theta_{diaz}^N \frac{PC_{diaz}^{photo}}{\alpha_{diaz} \theta_{diaz}^C I_{PAR}}$$

Particulate Terms (implicit)

Non-iron particulate terms:

Production:

$$\begin{aligned}
 POC^{prod} &= SP_{agg} + G_{sp}^{POC} + SP_{loss}^{POC} + Diat_{loss}^{POC} + Diat_{agg} + G_{diat}^{POC} + G_{diaz}^{POC} + F_Z^{POC} Z_{loss} \\
 PCaCO_3^{prod} &= \left((1 - f_{graz}^{CaCO_3, remin}) G_{sp} + SP_{loss} + SP_{agg} \right) Q_{sp}^{CaCO_3} \\
 PSiO_3^{prod} &= \left((1 - f_{graz}^{Si, remin}) G_{diat} + Diat_{agg} + f_{diat loss}^{POC} Diat_{loss} \right) Q_{diat}^{Si} \\
 free\ POC^{prod} &= POC^{prod} - \omega_{PCaCO_3} PCaCO_3^{prod} - \omega_{PSiO_3} PSiO_3^{prod}
 \end{aligned}$$

Vertical fluxes as function of depth (z):

$$\begin{aligned}
 soft\ PCaCO_3^{flux}(z) &= soft\ PCaCO_3^{flux}_{z_0} e^{\frac{-(z-z_0)}{\lambda_{PCaCO_3}}} + \left(1 - f_{PCaCO_3}^{hard} \right) \int_{z_0}^z PCaCO_3^{prod} e^{\frac{-(z-z_0)}{\lambda_{PCaCO_3}}} dz \\
 hard\ PCaCO_3^{flux}(z) &= hard\ PCaCO_3^{flux}_{z_0} e^{\frac{-(z-z_0)}{\lambda_{hard}}} + f_{PCaCO_3}^{hard} \int_{z_0}^z PCaCO_3^{prod} dz \\
 soft\ PSiO_3^{flux}(z) &= soft\ PSiO_3^{flux}_{z_0} e^{\frac{-(z-z_0)}{\lambda_{PSiO_3}} T_f^{SiO_3}} + \left(1 - f_{PSiO_3}^{hard} \right) \int_{z_0}^z PSiO_3^{prod} e^{\frac{-(z-z_0)}{\lambda_{PSiO_3}} T_f^{SiO_3}} dz \\
 hard\ PSiO_3^{flux}(z) &= hard\ PSiO_3^{flux}_{z_0} e^{\frac{-(z-z_0)}{\lambda_{hard}}} + f_{PSiO_3}^{hard} \int_{z_0}^z PSiO_3^{prod} dz \\
 soft\ dust^{flux}(z) &= \left(1 - f_{dust}^{hard} \right) \left(1 - f_{dust}^{bio} \right) dust_{z_0}^{flux} e^{\frac{-(z-z_0)}{\lambda_{dust}}} \\
 hard\ dust^{flux}(z) &= f_{dust}^{hard} \left(1 - f_{dust}^{bio} \right) dust_{z_0}^{flux} e^{\frac{-(z-z_0)}{\lambda_{hard}}} \\
 free\ POC^{flux}(z) &= free\ POC_{z_0}^{flux} e^{\frac{-(z-z_0)}{\lambda_{POC}} T_f^{POC}} + \int_{z_0}^z free\ POC^{prod} e^{\frac{-(z-z_0)}{\lambda_{POC}} T_f^{POC}} dz \\
 ballast\ POC^{flux}(z) &= \omega_{PCaCO_3} \left(soft\ PCaCO_3^{flux}(z) + hard\ PCaCO_3^{flux}(z) \right) \\
 &\quad + \omega_{PSiO_3} \left(soft\ PSiO_3^{flux}(z) + hard\ PSiO_3^{flux}(z) \right) + \omega_{dust} \left(soft\ dust^{flux}(z) + hard\ dust^{flux}(z) \right)
 \end{aligned}$$

Note: $free\ POC = soft\ POC$

Remineralization from conservation:

$$\begin{aligned}
 PCaCO_3^{remin}(z) &= PCaCO_3^{prod}(z) + \frac{d \left(soft\ PCaCO_3^{flux} \right)}{dz}(z) + \frac{d \left(hard\ PCaCO_3^{flux} \right)}{dz}(z) \\
 PSiO_3^{remin}(z) &= PSiO_3^{prod}(z) + \frac{d \left(soft\ PSiO_3^{flux} \right)}{dz}(z) + \frac{d \left(hard\ PSiO_3^{flux} \right)}{dz}(z) \\
 POC^{remin}(z) &= POC^{prod}(z) + \frac{d \left(free\ POC^{flux} \right)}{dz}(z) + \frac{d \left(ballast\ POC^{flux} \right)}{dz}(z) \\
 dust^{remin}(z) &= \frac{d \left(soft\ dust^{flux} \right)}{dz}(z) + \frac{d \left(hard\ dust^{flux} \right)}{dz}(z)
 \end{aligned}$$

Where:

$$T_f^{SiO_3} =_{SiO_3} q_{10}^{\frac{(T+T_{K0})-(T_{ref}+T_{K0})}{10}}; \quad T_f^{POC} =_{POC} q_{10}^{\frac{(T+T_{K0})-(T_{ref}+T_{K0})}{10}}$$

Particulate iron terms:

Production:

$$PFe^{prod} = (SP_{agg} + G_{sp}^{POC} + SP_{loss}^{POC}) Q_{sp}^{Fe} + (Diat_{loss}^{POC} + Diat_{agg} + G_{diat}^{POC}) Q_{diat}^{Fe} + G_{diaz}^{POC} Q_{diaz}^{Fe} + F_Z^{POC} Z_{loss} Q_Z^{Fe} + f_{scv}^{PFe} s^{Fe} Fe$$

Remineralization:

$$PFe^{remin}(z) = \begin{cases} POC^{remin}(z) R_{Fe:C} & : \text{free } POC^{flux}(z) + \text{ballast } POC^{flux}(z) = 0 \\ POC^{remin}(z) \frac{PFe^{flux}(z)}{\text{free } POC^{flux}(z) + \text{ballast } POC^{flux}(z)} & : \text{free } POC^{flux}(z) + \text{ballast } POC^{flux}(z) > 0 \end{cases}$$

Vertical flux from conservation:

$$\frac{d(PFe^{flux})}{dz}(z) = PFe^{prod}(z) - PFe^{remin}(z)$$

Total particulate Fe remineralization:

$$PFe^{remin}(z) = PFe^{remin}(z) + c_{dust}^{Fe} dust^{remin}(z)$$

Where:

$$s^{Fe} = f(s_0^{Fe})$$

Summary Features

- Fixed C/N/P ratios for phytoplankton and zooplankton.
- Fixed Fe/C ratio for zooplankton
- Variable Fe/C and Chl/C ratios for phytoplankton → explicit C, Fe and Chl pools for phytoplankton.
- Variable Si/C ratio for diatoms → explicit Si pool for diatoms.
- Variable C/N/P/Fe/Si ratios for DOM → explicit N, P, Fe and Si pools for DOM.
- Variable Fe/C and Si/C ratios implemented with losses at current cell ratios and uptake at a “growth ratio” that is a function of ambient nutrient conditions and the half-saturation constant for the group.

Model Parameters

Parameter	Value	Units	Definition
α	0.3	mmol C m ² (mg Chl W d) ⁻¹	initial slope of $P - I$ curve
α_{diaz}	0.036	mmol C m ² (mg Chl W d) ⁻¹	initial slope of $P - I$ curve for diazotrophs
T_{ref}	30	°C	reference temperature
T_{K0}	273.16	K	zero point for Celcius
q_{10}	2		temperature dependence factor
PC^{ref}	3.0	d ⁻¹	max. phyto. C-specific growth rate at T_{ref}
PC_{diaz}^{ref}	0.4	d ⁻¹	max. diazotrophs C-specific growth rate at T_{ref}
$K_{sp}^{NO_3}$	0.5	mmol N m ⁻³	small phyto. NO ₃ half saturation coefficient
$K_{sp}^{NH_4}$	0.005	mmol N m ⁻³	small phyto. NH ₄ half saturation coefficient
K_{sp}^{Fe}	6×10^{-5}	mmol Fe m ⁻³	small phyto. Fe half saturation coefficient
$K_{sp}^{PO_4}$	3.125×10^{-4}	mmol PO ₄ m ⁻³	small phyto. PO ₄ half saturation coefficient
$K_{diat}^{NO_3}$	2.5	mmol N m ⁻³	diatom NO ₃ half saturation coefficient
$K_{diat}^{NH_4}$	0.08	mmol N m ⁻³	diatom NH ₄ half saturation coefficient
K_{diat}^{Fe}	1.5×10^{-4}	mmol Fe m ⁻³	diatom Fe half saturation coefficient
$K_{diat}^{PO_4}$	0.005	mmol PO ₄ m ⁻³	diatom PO ₄ half saturation coefficient
$K_{diat}^{SiO_3}$	1.0	mmol SiO ₃ m ⁻³	diatom Si half saturation coefficient
$K_{diaz}^{PO_4}$	0.005	mmol PO ₄ m ⁻³	diazotrophs PO ₄ half saturation coefficient
K_{diaz}^{Fe}	1×10^{-4}	mmol Fe m ⁻³	diazotrophs Fe half saturation coefficient
η	0.06	d ⁻¹	nitrification rate
r	0.01	d ⁻¹	DOM remineralization rate
m_{sp}	0.1	d ⁻¹	small phyto. linear mortality rate
m_{diat}	0.1	d ⁻¹	diatom linear mortality rate
p_{sp}	0.009	(mmol C) ⁻¹ m ³ d ⁻¹	small phyto. quadratic mortality rate
p_{diat}	0.009	(mmol C) ⁻¹ m ³ d ⁻¹	diatom quadratic mortality rate
m_{diaz}	0.16	d ⁻¹	diazotrophs linear mortality rate
e_{sp}^{POC}	0.22	(mmol C) ⁻¹	small phyto. grazing factor
α_{sp}^{max}	0.2	d ⁻¹	max. aggregation rate for small phyto.
α_{diat}^{max}	0.2	d ⁻¹	max. aggregation rate for diatoms
α_{diat}^{min}	0.01	d ⁻¹	min. aggregation rate for diatoms
u_{max}^{sp}	2.75	d ⁻¹	max. zoo. growth rate on small phyto. at T_{ref}
u_{max}^{diat}	2.07	d ⁻¹	max. zoo. growth rate on diatoms at T_{ref}
u_{max}^{diaz}	1.2	d ⁻¹	max. zoo. growth rate on diazotrophs at T_{ref}
m_z	0.1	d ⁻¹	zoo. linear mortality rate
p_z	0.45	(mmol C) ⁻¹ m ³ d ⁻¹	zoo. quadratic mortality rate
g	1.05	mmol C m ⁻³	zoo. grazing coefficient
$max\theta_{sp}^N$	2.3	mg Chl (mmol N) ⁻¹	small phyto. max. Chl:N ratio
$max\theta_{diat}^N$	3.0	mg Chl (mmol N) ⁻¹	diatom max. Chl:N ratio
$max\theta_{diaz}^N$	3.4	mg Chl (mmol N) ⁻¹	diazotrophs max. Chl:N ratio
κ_{chl}	3×10^{-4}	cm ⁻¹ (mg Chl) ⁻¹ m ³	chlorophyll attenuation coefficient
κ_w	4×10^{-4}	cm ⁻¹	water attenuation coefficient
ϕ	0.45		PAR fraction of total irradiance

Model Parameters (continuation)

Parameter	Value	Units	Definition
ζ_C^N	1.43		ratio of N fixation to C fixation
Q	0.137		phyto. and zoo. N:C ratio
Q^P	0.00855		small phyto., diatom and zoo. P:C ratio
Q_{diaz}^P	0.002735		diazotroph P:C ratio
Q_Z^{Fe}	2.5×10^{-6}		zoo. Fe:C ratio
Q_{diat}^{Si}	0.137		initial diatom Si:C ratio
Q_{diat}^{Fe}	6×10^{-6}		initial diatom Fe:C ratio
Q_{sp}^{Fe}	6×10^{-6}		initial small phyto. Fe:C ratio
Q_{diaz}^{Fe}	42×10^{-6}		initial diazotrophs Fe:C ratio
Q_{max}^{Si}	0.685		max diatom Si:C ratio
i_z	0.3		zoo. ingestion coefficient (non-dim)
f_{DOC}^{lab}	0.70		fraction of loss to DOC that is routed directly to DIC
$f_{graz}^{sp,DOC}$	0.34		fraction small phyto. grazing to DOC
$f_{graz}^{sp,DIC}$	$1 - (i_z + f_{graz}^{sp,DOC})$		fraction of grazing on small phyto. routed to DIC
f_z^{diat}	0.81		scaling factor for grazing on diatoms
$f_{graz}^{diat,POC}$	0.26		fraction of diatom grazing routed to POC
$f_{graz}^{diat,DOC}$	0.13		fraction of diatom grazing routed to DOC
$f_{graz}^{diat,DIC}$	$1 - (i_z + f_{graz}^{diat,POC} + f_{graz}^{diat,DOC})$		fraction of diatom grazing routed to DIC
$f_{diat\ loss}^{POC}$	0.05		fraction of diatom loss routed to POC
$f_{diat\ loss}^{DOC}$	$1 - f_{diat\ loss}^{POC}$		fraction of diatom loss routed to DOC
$f_{graz}^{diaz,Z}$	0.21		fraction of diazotrophs grazing routed to zoo.
$f_{graz}^{diaz,POC}$	0.0		fraction of diazotrophs grazing routed to POC
$f_{graz}^{diaz,DOC}$	0.24		fraction of diazotrophs grazing routed to DOC
$f_{graz}^{diaz,DIC}$	$1 - (f_{graz}^{diaz,Z} + f_{graz}^{diaz,POC} + f_{graz}^{diaz,DOC})$		fraction of diazotrophs grazing routed to DIC
$f_{z\ loss}^{sp,POC}$	0.06666		fraction of zoo. losses routed to POC when eating small phyto.
$f_{z\ loss}^{diat,POC}$	0.1333		fraction of zoo. losses routed to POC when eating diatoms
$f_{z\ loss}^{diaz,POC}$	0.03333		fraction of zoo. losses routed to POC when eating diazotrophs
$f_{graz}^{CaCO_3,POC}$	0.4		min. proportionality between $Q_{sp}^{CaCO_3}$ and grazing losses to POC
$f_{graz}^{sp,POC}$	0.24		upper limit on fraction of grazing on small phyto. routed to POC
$f_{graz}^{CaCO_3,remin}$	0.33		fraction of SP_{CaCO_3} grazing which is remineralized
$f_{graz}^{Si,remin}$	0.5		fraction of diatom Si grazing which is remineralized
$f_{prod}^{sp,CaCO_3}$	0.026		fraction of small phyto. production as CaCO ₃ production
$R_D^{C:O_2}$	117/170		dissolved matter C:O ₂ ratio
$R_P^{C:O_2}$	117/170		particulate matter C:O ₂ ratio
$diaz\ R_D^{C:O_2}$	117/150		diazotrophs C:O ₂ ratio
$R_{Fe:C}$	3×10^{-6}		Fe:C ratio

Parameters for Particulate Equations

Parameter	Value	Units	Definition
$SiO_3 q_{10}$	4		temperature dependence factor for particulate SiO_3 remin.
$POC q_{10}$	1.12		temperature dependence factor for POC remin.
M_{POC}	12.01	g	POC molar mass
M_{CaCO_3}	100.09	g	$CaCO_3$ molar mass
M_{SiO_3}	60.08	g	SiO_3 molar mass
M_{dust}	1×10^9	g	dust molar mass
M_{Fe}	55.847	g	Fe molar mass
ω_{PCaCO_3}	$0.07 \times \frac{M_{CaCO_3}}{M_{POC}}$		qualitative associated POC/ $CaCO_3$ mass ratio for particulate matter
ω_{PSiO_3}	$0.035 \times \frac{M_{POC}}{M_{SiO_3}}$		qualitative associated POC/ SiO_3 mass ratio for particulate matter
ω_{dust}	$0.07 \times \frac{M_{dust}}{M_{POC}}$		qualitative associated POC/dust mass ratio for particulate matter
λ_{POC}	13000	cm	remineralization length scale for “soft” particulate POC
λ_{CaCO_3}	60000	cm	remineralization length scale for “soft” particulate $CaCO_3$
λ_{SiO_3}	2200	cm	remineralization length scale for “soft” particulate SiO_3
λ_{dust}	60000	cm	remineralization length scale for “soft” dust
λ_{hard}	4×10^6	cm	remineralization length scale for all “hard” particulate subclasses
$f_{PCaCO_3}^{hard}$	0.55		fraction of particulate $CaCO_3$ production routed to “hard” subclass
$f_{PSiO_3}^{hard}$	0.37		fraction of particulate SiO_3 production routed to “hard” subclass
f_{dust}^{hard}	0.97		fraction of surface dust flux routed to “hard” subclass
f_{dust}^{bio}	0.02		fraction of surface iron dust flux that is bioavailable
f_{scv}^{PFe}	0.1		fraction of Fe scavenging routed to particulate Fe
s_0^{Fe}	0.12	% of ambient	initial Fe scavenging rate
w_{dust}^{Fe}	0.035	g/g	Fe/dust weight ratio
c_{dust}^{Fe}	$\frac{w_{dust}^{Fe}}{M_{Fe}} \times 10^9$	nmol Fe/g dust	dust to iron conversion factor